

Math 739: Problem Set 2

Due on Friday, February 5

Be sure to prove all your answers.

1. p. 29, #1-7
2. p. 29, #1-9
3. p. 36, #2.8
4. p. 38, #2.10
5. Let S_n denote the set of permutations on n letters. Let each $\alpha \in S_n$ act on $S^1 \times S^1 \times \dots \times S^1$ (n times) by permuting the entries according to the permutation α .
 - (a) Show that this forms a *group action* of S_n on $S^1 \times \dots \times S^1$.
 - (b) Is this group action by diffeomorphisms? Prove your answer.
6. Consider the map

$$\begin{aligned} S^1 \times S^1 &\rightarrow S^1 \\ (t_1, t_2) &\rightarrow t_1 t_2^{-1}. \end{aligned}$$

Is this a Lie group homomorphism? Is it smooth? What is its kernel?