MATH 250 FINAL EXAM REVIEW SHEET

Chapter 2. First order equations

• Integrating factor (2.1)

- Separable equations (2.2)
 - \circ $\;$ Review exlicit form of solution for IVP $\;$
 - \circ Review integration (see #7 on Exam 1)

Chapter 3. Second order linear equations

Linear equations with constant coefficients (3.2, 3.4, 3.5)

- Characteristic equation and its roots
- \circ Finding general solution for all cases (see summary p.165)

<u>Reduction of order (3.5)</u>

• <u>Method of undetermined coefficients (3.6)</u>

- Finding the form of a particular solution (see table p.175)
- Determining coefficients in the particular solution
- \circ $\;$ Finding the general solution of a nonhomogeneous equation

• Mechanical vibrations (3.8, 3.9)

- Setting up and solving free or forced spring-mass system
- Review methods for finding k and γ
- Review "beat" vs. resonance

Chapter 6. Laplace transform

- <u>Solution of IVP (6.2, 6.4)</u>
 - Make sure you know how to use the Table on p.304 (it will be provided)
 - Review partial fractions, factoring and completing the square techniques
- Step functions (6.3)
 - Review definition of a step function, finding values of piecewise cts functions
 - \circ $\;$ Taking direct and inverse Laplace trasform of functions given in terms of step functions $\;$
 - Remember that e.g. $L(tu_2(t)) \neq L(t) \cdot L(u_2(t))$! Review formula 13 from the Table.
 - Make sure you know how to solve ##7-18 on p.314, ##1-13, p.321

Chapter 7. Systems of ODEs

- Equivalence of an n-th order ODE and a system of n 1st order ODEs (7.1)
 - \circ $\;$ Review techniques of converting system into a single equation and back

Solving homogeneous linear systems with const coefficients (7.5, 7.6)

- Finding eigenvalues and eigenvectors of a 2x2 matrix
- Writing general solution for distinct real and complex roots (in real-valued functions)
- Solving IVPs
- o Classification of critical points (node, saddle or spiral) and stability
- o Basic strategies in graphing phase portraits