

MATH 110 – QUIZ 12 – 16 NOVEMBER 2006

Answer all of the following questions in the space provided.

1. A fair coin is tossed three times and the number of heads is observed.

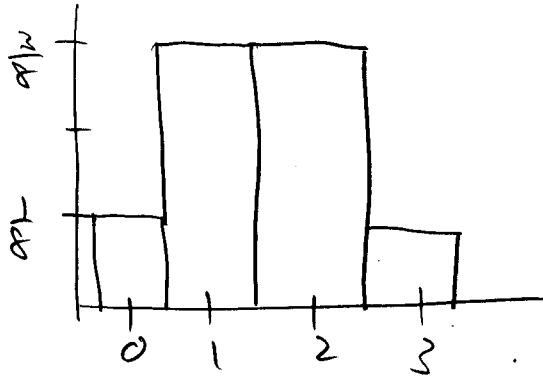
(a) (4 pts.) Determine the probability distribution for this experiment and draw its histogram.

$$\Pr(0 \text{ heads}) = \frac{1}{8}$$

$$\Pr(1 \text{ head}) = \frac{3}{8}$$

$$\Pr(2 \text{ heads}) = \frac{3}{8}$$

$$\Pr(3 \text{ heads}) = \frac{1}{8}$$



(b) (3 pts.) Define the random variable X by $X =$ “the number of heads observed in three tosses of a fair coin.” Write down a table giving the probability distribution for this random variable.

k	$\Pr(X=k)$
0	$1/8$
1	$3/8$
2	$3/8$
3	$1/8$

(c) (3 pts.) Write down a table giving the probability distribution for the random variable $(X-1)^2$, where X is the random variable defined in part (b).

k	$\Pr((X-1)^2=k)$
0	$3/8$ ← Since $(X-1)^2=0$ means $X=1$
1	$4/8$ ← Since $(X-1)^2=1$ means $X=0$ or $X=2$
4	$1/8$ ← Since $(X-1)^2=4$ means $X=3$