

Homework 4a

This homework problem is due on Thursday, June 18, the day of the final.

Use separation of variables to find a solution to the Laplace's equation.

$$\begin{aligned}u_{xx} + u_{yy} &= 0 \text{ on } (0, a) \times (0, b) \\u(0, y) &= 0, \\u(a, y) &= 0, \\u(x, 0) &= 0, \\ \text{and } u_y(x, b) &= f(x).\end{aligned}$$

Solve this in general, and write a specific solution when $f(x) = x$.