

§ 2.2 Homework Solutions

2) a) b) [BB] c) $\mathbb{Z} \cap (S \cup T) = \{2, 4, 5, 6, 25\} = (\mathbb{Z} \cap S) \cup (\mathbb{Z} \cap T)$ (they are equal).

d) $\mathbb{Z} \cup (S \cap T) = \{-2, -1, 0, 1, \sqrt{2}, 2, 3, \dots\} = (\mathbb{Z} \cup S) \cap (\mathbb{Z} \cup T)$ (they are equal).

4) $A = \{(1,1), (1,2), (2,2), (1,3), (2,3), (3,3)\}$, $B = \{1, -1, 2, -2\}$ (removing the repeats)

10) a) b) [BB] c) $M \cap P \neq \emptyset$ d) $(C \cap T^c) \subseteq P$ e) $((M \cup C) \cap P) \subseteq T^c$

12) a) [BB] b) $0 \in \mathbb{Z} \setminus \mathbb{N}$ c) $\mathbb{N} \subseteq \mathbb{Z}$ d) $\mathbb{Z} \not\subseteq \mathbb{N}$ \Rightarrow

16) a) A is a subset of B, i.e. $A \subseteq B$ b) $A \cup B = A \Rightarrow B \subseteq A$

17) [BB]

27) a) [BB] b) No. A counterexample is $A = \{1\}$, $B = \{2\}$, $C = \{3\}$

c)

Yes. Let $x \in B$

Case 1) Suppose $x \in A \Rightarrow x \in A \oplus B \Rightarrow x \in A \oplus C \Rightarrow x \in C$

Case 2) Suppose $x \notin A \Rightarrow x \in A \oplus B \Rightarrow x \in A \oplus C \Rightarrow x \in C$

The above proves that $B \subseteq C$. Reversing the B and C proves $C \subseteq B$.
Thus $B = C$.

d) False. A may be \emptyset .