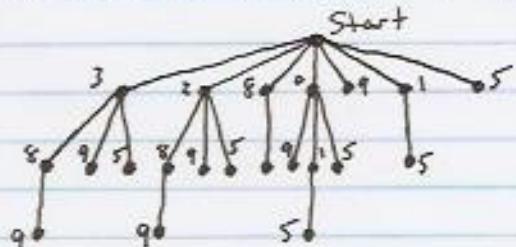


312.1 Homework Solutions

1) [BB]

3) There are 13 in total: 7 at level 1, 11 at level 2, 3 at level 3



13) a) [BB]

b) 3, one corresponding to each tree in a)

15) [BB]

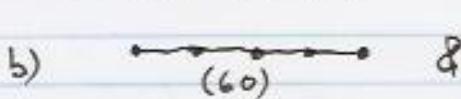


(+ different labelled trees isomorphic to this)

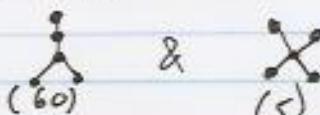
&

(12 different labelled trees isomorphic to this one)

$$\& 12 + 4 = 16 = 4^{4-2} \quad \checkmark$$



&



$$60 + 60 + 5 = 5^{5-3} \quad \checkmark$$

24) We use induction on n :

Step 2: Result is clearly true for $n=1$

Step 1: Inductive Hypothesis — suppose result is true for all trees with k vertices.

Let T be a tree with $k+1$ vertices.

Then \exists vertex v in T with $\deg(v) = 1$

Then $T \setminus \{v\}$ is a (connected) tree with k vertices

\therefore By Inductive Hypothesis $T \setminus \{v\}$ is bipartite

So placing v in opposite partition set to its neighbouring vertex
 $\Rightarrow T$ is bipartite. So $P_k \Rightarrow P_{k+1}$.

Result holds by Mathematical Induction