

## Introduction to Trigonometry Worksheet

### Degrees, Radians and Special Triangles

1. Give the complement and supplement of each angle

a.  $40^\circ$

b.  $110^\circ$

c.  $\theta$

2. Covert  $45^\circ$  to radians

3. Covert  $450^\circ$  to radians

4. Covert  $\frac{\pi}{6}$  to degrees.

5. Covert  $\frac{4\pi}{3}$  to degrees.

6. If the shortest side of a  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle is 5, find the other two sides.

7. A ladder is leaning against a wall. The top of the ladder is 4 feet above the ground and the bottom of the ladder makes an angle of  $60^\circ$  with the ground. How long is the ladder, and how far from the wall is the bottom of the ladder?

## Trigonometric Functions

1. Find the sine and cosine of  $45^\circ$ .

2. Find the sine, cosine and tangent of  $\frac{\pi}{3}$ .

3. Find the six trigonometric functions of  $\theta$  if  $\theta$  is in standard position and the point  $(-2, 3)$  is on the terminal side of  $\theta$ .

4. Find the six trigonometric ratios of  $\frac{3\pi}{2}$ .

5. If  $\sin \theta = -\frac{5}{13}$ , and  $\theta$  terminates in quadrant III, find  $\cos \theta$  and  $\tan \theta$ .

### Graphing: Amplitude and Period

1. Sketch the graph of  $y = \cos x$ .
2. Sketch the graph of  $y = 2\sin x$  for  $0 \leq x \leq 2\pi$ .
3. Sketch one complete cycle of the graph of  $y = \frac{1}{2}\cos x$ .
4. Graph  $y = \sin 2x$  for  $0 \leq x \leq 2\pi$ .
5. Sketch the graph of  $y = \csc x$

### Graphing: Phase Shift

1. Sketch the graph of  $y = \sin\left(x + \frac{\pi}{2}\right)$  if  $-\frac{\pi}{2} \leq x \leq \frac{3\pi}{2}$ .

2. Graph on complete cycle of  $y = \sin\left(x - \frac{\pi}{2}\right)$ .

3. Graph  $y = 2\cos(3x + \pi)$  from  $x = -\frac{2\pi}{3}$  to  $x = \frac{2\pi}{3}$ .

4. Graph on complete cycle of  $y = 4\sin\left(2x - \frac{\pi}{3}\right)$ .

## Inverse Trigonometric Functions

1. Evaluate in radians without using a calculator or tables

a.  $\sin^{-1} \frac{1}{2}$

b.  $\arccos \left( -\frac{\sqrt{3}}{2} \right)$

c.  $\tan^{-1}(-1)$

2. Evaluate  $\sin \left( \tan^{-1} \frac{3}{4} \right)$  without using a calculator.

3. Evaluate

a.  $\sin^{-1} \left( \frac{\sqrt{3}}{2} \right)$

b.  $\tan^{-1}(1)$

c.  $\sin^{-1} \left( -\frac{1}{2} \right)$

d.  $\tan \left( \sin^{-1} \frac{3}{5} \right)$