

MATH 108 – 21 FEBRUARY 2011– EXAM 1

Answer each of the following questions. Show all work, as partial credit may be given.

1. (10 pts.) A cylindrical soda can has a volume of  $7\pi$  cubic inches. Express the surface area of the can as a function of its radius. (Hint: The formula for the volume of a cylinder of radius  $r$  and height  $h$  is  $V = \pi r^2 h$ , and the surface area of a closed cylinder is  $S = 2\pi r h + 2\pi r^2$ .)

2. (10 pts. each) Compute each of the following limits.

(a)  $\lim_{x \rightarrow 3} \frac{9 - x^2}{x - 3}$

(b)  $\lim_{x \rightarrow \infty} \frac{2x + 3}{x^2 + 1}$

3. Let  $f(x) = \begin{cases} \frac{x^2 + 1}{x + 1} & \text{if } x < 1 \\ 2 - x^3 & \text{if } x \geq 1 \end{cases}$ .

(a) (10 pts.) Compute the one-sided limits  $\lim_{x \rightarrow 1^+} f(x)$  and  $\lim_{x \rightarrow 1^-} f(x)$ .

(b) (5 pts.) Is  $f(x)$  continuous at  $x = 1$ ? Why or why not?

4. (10 pts.) Evaluate  $\lim_{x \rightarrow 2^+} \frac{x^2 + 1}{2x - 4}$  by indicating whether it is  $+\infty$  or  $-\infty$ .

5. (10 pts.) Find the equation of the tangent line to the graph of the function  $f(x) = 2 - x^3$  at  $x = 1$ .

6. (10 pts.) After  $x$  weeks, the number of people using a new rapid transit system was approximately  $N(x) = 6x^3 + 500x + 8000$ . At what rate was the use of the system changing after 8 weeks? Is the usage increasing or decreasing at this time?

7. (10 pts. each) Evaluate the following derivatives using whatever method you like. Be sure to simplify your answer.

(a)  $f(x) = (2 + 5x)^{1/2}$

(b)  $y = x^2(2x + 3)^5$

(c)  $g(t) = \frac{x}{2 - x}$ .